## Homework 3

## 9/16/22

## Homework 3 is due 9/23/2022 at 11:59 PM. Submit your homework on Canvas as one PDF document.

The PDF version of this assignment can be found here.

- 1. Let  $X_1, X_2, \dots, X_n \stackrel{iid}{\sim} N(\mu, \sigma^2)$  and  $Z_i = \frac{X_i \mu}{\sigma}$ . Find the distribution of  $Y = \sum_{i=1}^n Z_i^2$ .
- 2. Let  $X_1, X_2, \ldots, X_n \stackrel{iid}{\sim} N(\mu, \sigma^2)$  and  $a_1, a_2, \ldots, a_n$  be a set of known constants. Find the distribution of  $Y = \sum_{i=1}^n a_i X_i$ .
- 3. Let  $X_1 \sim Bin(n_1,p)$  and  $X_2 \sim Bin(n_2,p)$ . Find the distribution function of  $Y = X_1 + X_2$ . Assume  $X_1 \perp X_2$ .